

APPENDIX A

AFFINITY LAWS, MODEL RELATIONSHIPS AND GENERATOR SPEEDS  
VERSUS NUMBER OF POLES

<u>SECTION</u>	<u>SUBJECT</u>	<u>PAGE</u>
A1	PUMP AFFINITY LAWS	A-3
A2	PUMP MODEL RELATIONSHIPS	A-3
A3	TURBINE AFFINITY LAWS	A-4
A4	TURBINE MODEL RELATIONSHIPS	A-5
A5	GENERATOR SPEEDS VS. NUMBER OF POLES	A-6

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# A1. PUMP AFFINITY LAWS

## With Impeller Diameter Held Constant

$$\frac{Q_1}{Q_2} = \frac{N_1}{N_2}$$

$$\frac{H_1}{H_2} = \left( \frac{N_1}{N_2} \right)^2$$

$$\frac{Bhp_1}{Bhp_2} = \left( \frac{N_1}{N_2} \right)^3$$

## With Speed Held Constant

$$\frac{Q_1}{Q_2} = \frac{D_1}{D_2}$$

$$\frac{H_1}{H_2} = \left( \frac{D_1}{D_2} \right)^2$$

$$\frac{Bhp_1}{Bhp_2} = \left( \frac{D_1}{D_2} \right)^3$$

# A2. PUMP MODEL RELATIONSHIPS

$$\frac{N_1}{N_2} = \frac{D_2}{D_1} \times \left( \frac{H_1}{H_2} \right)^{1/2}$$

$$\frac{Q_1}{Q_2} = \left( \frac{D_1}{D_2} \right)^2 \times \left( \frac{H_1}{H_2} \right)^{1/2}$$

$$\frac{P_1}{P_2} = \left( \frac{H_1}{H_2} \right)^{3/2} \times \left( \frac{D_1}{D_2} \right)^2$$

$$\frac{H_1}{H_2} = \left( \frac{Q_1}{Q_2} \right)^{2/3} \times \left( \frac{N_1}{N_2} \right)^{4/3}$$

$$\frac{Q_1}{Q_2} = \frac{N_1}{N_2} \times \left( \frac{D_1}{D_2} \right)^3$$

$$\frac{P_1}{P_2} = \left( \frac{N_1}{N_2} \right)^3 \times \left( \frac{D_1}{D_2} \right)^5$$

When  $H_1 = H_2$

Then  $\frac{H_1}{H_2} = \left( \frac{D_1}{D_2} \right)^2 \times \left( \frac{N_1}{N_2} \right)^2 = 1$

Therefore  $\frac{D_1}{D_2} = \frac{N_2}{N_1}$

Note: Subscript 1 refers to model pumps.  
Subscript 2 refers to prototype pumps.

$$\text{and} \quad \frac{Q_2}{Q_1} = \left( \frac{D_2}{D_1} \right)^3 \times \frac{N_2}{N_1} = \left( \frac{D_2}{D_1} \right)^3 \times \frac{D_1}{D_2} = \left( \frac{D_2}{D_1} \right)^2$$

$$\frac{P_2}{P_1} = \left( \frac{D_2}{D_1} \right)^5 \times \left( \frac{N_2}{N_1} \right)^3 = \left( \frac{D_2}{D_1} \right)^5 \times \left( \frac{D_1}{D_2} \right)^3 = \left( \frac{D_2}{D_1} \right)^2$$

$$N_s = \frac{N \times Q^{1/2}}{H^{3/4}} \quad \text{Where } Q \text{ is in gpm, } N \text{ is RPM, and } H \text{ is in feet.}$$

$$\text{whp} = \frac{W \times \text{CFS} \times H}{550} = \frac{S \times \text{GPM} \times H}{3960}$$

Where  $W$  is specific weight of water (lb/ft<sup>3</sup>)

$S$  is specific weight of liquid referred to water at 68°F

$H$  is turbine net head in feet

$$\text{eff} = \frac{\text{whp}}{\text{bhp}}$$

$$\sigma = \frac{\text{NPSH}}{H}$$

### A3. TURBINE AFFINITY LAWS

#### For Constant Diameter

$$\frac{P_1}{P_2} = \left( \frac{H_1}{H_2} \right)^{3/2}$$

$$\frac{N_1}{N_2} = \frac{Q_1}{Q_2} = \left( \frac{H_1}{H_2} \right)^{1/2}$$

#### For Constant Head

$$\frac{N_1}{N_2} = \frac{D_2}{D_1}$$

$$\frac{Q_1}{Q_2} = \left( \frac{D_1}{D_2} \right)^2 = \frac{P_1}{P_2}$$

#### A4. TURBINE MODEL RELATIONSHIPS

$$\frac{N_1}{N_2} = \frac{D_2}{D_1} \times \left( \frac{H_1}{H_2} \right)^{1/2}$$

$N_R$  = Prototype Runaway Speed

$$N_R = \frac{1838 \times \phi \times (H_2)^{1/2}}{D_2}$$

$$\frac{Q_1}{Q_2} = \frac{N_1}{N_2} \times \left( \frac{D_1}{D_2} \right)^3$$

$$\frac{HP_1}{HP_2} = \left( \frac{H_1}{H_2} \right)^{3/2} \times \left( \frac{D_1}{D_2} \right)^2$$

$$\frac{Q_1}{Q_2} = \left( \frac{D_1}{D_2} \right)^2 \times \left( \frac{H_1}{H_2} \right)^{1/2}$$

$$\frac{HP_1}{HP_2} = \left( \frac{N_1}{N_2} \right)^3 \times \left( \frac{D_1}{D_2} \right)^5$$

$$\sigma = \frac{H_b - H_v - H_s}{H}$$

Roger's Curve:  $\sigma = \frac{N_s^2}{16,000}$

$$\Phi = \frac{N \times D}{1838 \times H^{1/2}}$$

$$N_s = \frac{N \times P^{1/2}}{H^{5/4}}$$

$$Q = \frac{HP \times 8.8}{H \times \text{eff}}$$

Turbine Shaft Diameters:  $d = \frac{321,000 \times HP^{1/3}}{N \times \text{Stress}}$  (solid shafts)

Hollow Shafts:  $s = \frac{321,000 \times HP \times d}{N (d^4 - d_1^4)}$  ( $d_1$  is inside diameter)

A5. GENERATOR SPEEDS vs NUMBER OF POLES

$$\text{RPM} = \frac{120 \times \text{Hz}}{n} \quad \text{For 60 cycles: RPM} = \frac{7,200}{n}$$

Hz = Frequency in cycles per second

n = No. of Poles

60 Hz Synchronous Speeds

<u>Poles</u>	<u>RPM</u>	<u>Poles</u>	<u>RPM</u>	<u>Poles</u>	<u>RPM</u>
24	300.0	60	120.0	104	69.2
26	277.0	64	112.4	110	65.5
28	257.1	68	105.9	112	64.3
30	240.0	70	102.9	120	60.0
32	225.0	72	100.0	126	57.1
36	200.0	76	94.7	128	56.2
40	180.0	80	90.0	130	55.4
42	171.4	84	85.7	132	54.5
44	163.6	88	81.8	136	52.9
48	150.0	90	80.0		
50	144.0	96	75.0		
52	138.5	98	73.5		
56	128.6	100	72.0		

Note: Omit Poles 34, 38, 54, 58, 62, 66, 72, and 82.